

# Placing Servers in Overlay Networks

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## Abstract

Overlay networks are becoming a popular vehicle for deploying advanced network services in the Internet. Overlay networks are implemented by deploying *service nodes* at suitably chosen sites in the network. Service nodes communicate with users through the commodity Internet, while among themselves, they may use either the commodity Internet or dedicated channels. The number of distinct service nodes has a big influence on the operational cost of an overlay network; meanwhile, the distance between service nodes and end users has a big influence on the quality of the service. In this paper, we study the problem of how to optimally place service nodes in a network, balancing the need to minimize the number of nodes, while limiting the distance between users and service nodes. We show that the design problem is NP-hard and study the performance of heuristic algorithms using simulation. For single domain, our algorithms produce results that are within a few percent of an easily computed lower bound. For multi-domain networks, the performance ranges from close to the optimal to roughly twice the optimal.

## Keywords

overlay network, quality-of-service, set cover, integer programming, facility location

## 1 Introduction

As the explosive growth of the Internet continues, service providers are pushing more network functions towards the network edges to reduce client access latency and achieve better scalability. This distributed server

model is often referred to as overlay network, since servers form an overlay of unicast connections to cooperate and communicate among themselves. Content providers, such as Akamai [1] and iBeam [12] are among the first to deploy an overlay network of content distribution servers. Newer value-added services such as Active Networks, also adopt the overlay network approach. In an overlay network, both the communication channels between servers and clients and among servers are through the commodity Internet. However, while the server-to-server paths can be explicitly provisioned to carry the traffic, the resource management and reservation on the client access paths are far more costly and are typically not done. Consequently, the quality of the services are determined largely by network locations of deployed servers.

The current Internet has thousands of ISPs. In order to serve more clients, servers are placed strategically at the peering points of these networks to interconnect with as many ISPs as possible. However, operating and maintaining these distributed servers represents a major cost for service providers and limits the number of servers that can be deployed. Additionally, as the number of servers grows large, the cost of interconnecting these servers for data and state synchronization also increases.

In this paper, we attempt to answer the following questions: *Given multiple networks and their interconnections, how many servers are needed and where to locate them, so that service providers can ensure service qualities to all clients.* The imposition of the service quality constraints on server to client paths is an important aspect of this server placement problem, as we envision that it is essential for the newer network services to achieve better service quality in order to attract and retain customers. The measure of service quality varies from application to application, it can be delay for real-time applications, or bandwidth for content distribution applications, or a combination of both. Within an ISP network, the service provider can estimate these service quality parameters for a given client to a potential server location based on the client's network access technology and the capacities of the internal routing paths. Across the ISP domains, such estimation is achievable if networks cooperate and explicitly indicate in the routing messages the peering path taken by the given destination. Together with the inter-domain and the intra-domain estimations, the providers can then estimate the parameters. These mechanisms are variations of QoS routing mechanisms: instead of routing packets onto a path that has the desired resources, we estimate the resources on a known path. The details of these mechanisms are beyond the scope of this paper, hereby we assume that we can decide in advance whether or not a specific server can provide a given client with the guaranteed service. In this paper, we will simply use the network distance between a client and a server to make the decision, however, our methods can apply to any generic metrics.

To answer the above question, we transform the placement problem to the set cover problem [3] and solve it using both linear programming (LP) relaxation and greedy heuristics. Briefly, an instance of the set cover problem is that given a base set of elements and a family of sets that are subsets of the base set, find the minimum number of sets such that their union includes all elements in the base set. The set cover problem maps from the server placement problem as follows: the base element set contains all the network locations, which are the locations of network edge routers representing the aggregation of clients for a given network; A set represents a potential server placement at one of the network locations and its elements are all other network locations that are within the service range from the server. By solving the set cover problem, we find the minimum number of servers and their locations, that cover all clients within the service range. In this paper, we will only consider the uncapacitated version of the set cover problem, where the servers do not have capacity limits and can serve as many clients as possible. We think this uncapacitated version is adequate since it is typically cheaper to buy more bandwidth at one location than to install a separate server. The set cover problem is NP-Hard [16] and has worst case approximation ratio of  $O(\log n)$  [7]. Using simulation, we show that our combined rounding techniques and a simple pruning algorithm approach the lower bound very closely; in fact, it reaches the lower bound for a number of network configurations. Meanwhile, the greedy heuristic also provides good performance in all instances with significantly less computation complexity.

We also vary the problem to allow *primary* and *backup* servers. A primary server provides the guaranteed service to clients, while a backup server is allowed to provide a reduced level of service quality and functions only when the primary fails. Since more servers are qualified to function as backups, we can achieve better service reliability with only a slight increase on the total number of servers.

One important aspect of our study is the network modeling used in our simulation. Existing network modeling tools, such as GT-ITM [25] and Tiers [5], can generate hierarchical network graphs with probabilistic network interconnections, however, they do not explicitly model the geographical location of the networks. In our model, we consider the potential of co-located servers which can access multiple networks from the same geographical location; this mirrors the behavior of co-location service providers in the current Internet. Therefore, when two network nodes of different networks are within a geographical vicinity, an installation of server at this location can service clients, who are within the service range, in both networks. We show that these co-locations can reduce a large number of required servers, since they can avoid detours through the network peering points and provide shortcuts from one network to another.

The rest of the paper is organized as follows: in Section 2, we discuss some of the related work; we describe the two network models used in our simulation in Section 3; Section 4 introduce our methods using LP-relaxation and the greedy heuristic; We present simulation results in Section 5 and conclude in Section 6.

## 2 Related Work

The application of the set cover problem in network design has two variants: the facility location problem and the  $k$ -median problem. The facility location problem minimizes the joint cost of server installation and the cost of connecting each client to its designated server. This problem has been applied to designing and placing network concentrators. The  $k$ -median problem minimizes the cost of connections between clients and servers under the constraint that no more than  $k$  servers can be used. Both problems are NP-Hard. The best known approximation algorithms can achieve constant ratio [8, 14, 21], if the connection cost is symmetric and satisfies triangle inequality. For arbitrary cost, the worst case bound is  $O(\log n)$ . However, neither of the problems can be applied directly to the design of overlay networks, since in the overlay model the communication channels between clients and servers are over the commodity Internet and do not incur any cost to service providers. Rather, the major cost is the number of servers needed to service all clients and the access bandwidth required at each server's network interface.

Our model of server placement more closely resembles the set cover problem. The classic greedy algorithm for solving set cover problem [15, 17] achieves an  $O(\log n)$  performance ratio. In geometric spaces, the problem is easier. In [11], Hochbaum proposed a shifting strategy that gives an  $O(1 + \varepsilon)$  performance ratio. Unfortunately, the interconnections between networks dictate that the network propagation delay no longer exhibits the geometric properties of distance.

References [18, 19] studied the problem of placing cache replicas in the network and formulated it as the  $k$ -median problem: given a specific number of servers, what is the best placement that achieves the highest average service level to clients, where service level is indicated by access delay from a client to its nearest replica. In [18], Qiu et al. proposed several placement strategies including: a greedy strategy that incrementally places replicas to achieve highest service quality; a hot-spot strategy that places replicas near the clients that generate the greatest load. In [19], the authors also proposed a max degree strategy by placing replicas in decreasing order of nodes' degrees. By simulating over several synthetic and real network graphs, they concluded that the greedy strategy performs remarkably well, achieving within 1.1 to

1.5 of the lower bound.

Our approach to network design is from a different angle. We are more interested in examining the necessary cost, in this case the number of servers, if we want to provide all clients a guaranteed service. This gives service providers insight into the relation of network cost and the achievable service quality, on which they can make further adjustment to reflect their revenue stream, such as eliminating servers that only serve small numbers of clients. Contrarily, the work in [18, 19] seeks to optimize the average service quality which masks the number of unhappy customers. Additionally, the performance of our approach, which is the number of required servers, is not susceptible to the cost metric of connection paths, since we only use it to categorize clients as serviceable or not by a server; while theirs is achieved for a specific cost metric, namely the access delay. Since the connection cost metric depends heavily on the application, it is questionable if the same ratio could be achieved with a different metric.

Another difference is that we model the network geographically and consider server co-locations. As networks overlap geographically, the number of potential server locations is much fewer in number than the number of network nodes need to be considered. In [18, 19], they used network graphs consisting of tens of thousands nodes for router-level graphs and thousands of nodes for AS-level graphs. Consequently, the optimal algorithm based on LP relaxation is too expensive for their models. We think considering the geographical locations of servers is a reasonable approach given the vast presences of co-location providers. The reduced problem size enables us to solve it more optimally. In Section 5, we compare the performance of our algorithm both with co-location and without, and show that with co-location we can reduce the number of required servers to approximately half of that with no network co-locations.

### **3 Network Models**

It is a difficult task to model the Internet in a credible way, since it requires a large amount of information from thousands of network providers, most of which are not willing to fully disclose their network information. Earlier, topology generators such as the GT-ITM [25] and Tiers [5] create network graphs with hierarchies and probabilistic connectivities. Recent study from [6] shows that several network parameters, such as degree distribution, exhibit power-law properties instead of strong hierarchies. This spurs new topology generators such as BRITE [2] and Inet [13] to generate graphs with power law based node degree distribution. Furthermore, study from [22] shows that these power-law based generators seem to produce

network structures more representative of the Internet. However, the authors concede that such similarity depends largely on the comparison metric, among which there are no clear indication as the best to characterize the Internet. Additionally, the real network information obtained from the BGP routing tables plus the mapping from IP addresses to AS domains, are still far from complete to represent the Internet.

Given these difficulties, we think it is better to model the network with variations on network properties using simple network structures. This also has the advantage of allowing us to examine the relation between network parameters and the result; comparatively the Internet would be too complex a structure to extract any such insight.

We therefore model the networks using two types of graphs: random graphs and geographic graphs. The latter consists of network nodes located at the 50 largest US metropolitan areas. For inter-domain network connectivities, we specify a set of parameters to determine the location and density of network peering points. For intra-domain network connectivities, as ISPs are not willing to disclose fully their network topology, we have to assume that they are able to engineer and operate their own networks with little or no congestion internally so that the delay between routers are dominated by propagation delay. Consequently, we model the intra-domain network as a complete graph. We use the “hot-potato” routing policy at the inter-domain level, which minimizes the number of network domains crossed. Hence, traffic destined to another domain is always piped to the nearest peering points from the originator towards the destination domain. Although such policy does not result in the best global routes, it is widely used by the current inter-domain routing protocol: the Border Gateway Protocol (BGP) [20].

We realize our settings may not be very realistic, however, we are not aware of any information that allows us to model geographically the AS-level as well as the router-level networks. The Netgeo tool [23] from CAIDA is probably the closest tool trying to resolve this issue. It extracts information from the whois [9] database and attempts to map Internet hosts according to their domain names. But it is not clear to what extent this method is accurate especially when large IP address block can be assigned to a single entity and there is the possible inconsistency between whois databases. Additionally, it is also not possible to determine all the locations of network peering points as many ISPs have private peering links in addition to their point of presence at the public peering points such as at the MAEs and NAPs. We detail our settings for the two models below and summarize the parameters in Table 1.

Parameters	Interpretations
$n$	network size as # of nodes
$scale$	size of the network graph
$N_p$	probability of a city in a network
$TX_p$	interconnection probability between two networks
$TX_{scope}$	scope of a region for network interconnections
$TX_{ds}$	interconnection density
$vicinity$	maximum distance between co-located nodes

Table 1: Parameters for Generating Network Graphs

## Random Graph

In the random graph model, networks overlap each other on the same geometric space, whose size is defined by the  $scale$  parameter. The number of nodes in each network is uniformly drawn from the interval on  $[min, max]$ . We divide the network into fixed size of regions according to the parameter  $TX_{scope}$ ; nodes in different networks are allowed to peer with each other only if they are in the same region. The interconnection probability  $TX_p$  decides if a pair of networks interconnect; we choose  $TX_p$  based on the size of the two networks:

$$TX_p = \alpha e^{\beta \frac{\sqrt{n_1 n_2}}{max}}$$

where  $n_1$  and  $n_2$  are number of nodes in the two networks,  $\alpha$  and  $\beta$  are the scale and shape of the probability distribution, respectively.

If two networks interconnect, we randomly select a number of regions to interconnect according to the interconnection density  $TX_{ds}$ . If there are multiple nodes from each network in the same region, we select the closest pair of nodes as peers; if a region is selected, but one of the network does not have any node in that region, we choose another region until we met the peering density criterion, or we have considered all regions. We allow co-location nodes if nodes from different networks are in a geometric vicinity of each other. A server placed at a co-location can send traffic to all these networks with no additional cost.

## Geographic Graph

In the geographic model, we use the 50 largest metropolitan areas [24] as node locations. We then divide the US continent into 5 regions: northeast, north-central, southeast, south-central and west, and categorize nodes into each region with certain amount of overlap. Appendix A lists the categorization of the metro areas. Unlike the random graph model where all networks share the same geometric space, the geographic

model consists of two types of networks: regional networks and national networks. Each city joins the network with probability  $N_p$ : the selection of nodes for a regional network considers only nodes that belong to that region; while a national network considers all 50 cities. As before, we use  $TX_p$  to decide if two networks will interconnect, however,  $TX_p$  could be different depends on the type of the two networks, for example, two national networks will have  $TX_p = 1$ , since they are almost always interconnected; while two regional networks are less likely to peer with each other directly but to transit through a national network. We allow interconnections only if two network nodes are in the same city, as before, we use  $TX_{ds}$  to decide the number of peering points of two networks.

## 4 Formal Definitions and the Algorithms

Given our network models and routing policy, we can compute a routing table for each node  $i$  and the cost of each routing path  $c(i, j)$ , which is the summation of hop distances along the path. For each node  $i$ , we compute a set  $S$  which includes all the nodes reachable from  $i$  within the routing distance of  $C$ . If  $i$  has co-location nodes, then the set  $S$  also includes all nodes reachable from each of these co-location nodes within distance  $C$ . Let  $S_1, S_2, \dots, S_m$  be all the sets computed. An integer programming formulation of the set cover problem is:

$$\text{Objective: } \text{minimize } \sum_{j=1}^m x_j \quad (1)$$

$$\text{Subject to: } \sum_{j=1}^m a_{ij} x_j \geq 1 \quad \text{for } i = 1 \dots n \quad (2)$$

$$x_j \in \{0, 1\}$$

where  $x_j$  is the selection variable of  $S_j$ ,  $a_{ij}$  is 1 if  $i \in S_j$  and 0 otherwise.

A variation of the problem is to allow one primary and one backup server to cover each node. A backup server can cover twice the distance of the primary server. Let  $T_1, T_2, \dots, T_m$  be all the backup sets, and  $b_{ij} = 1$  if  $i \in T_j$  and 0 otherwise. The objective here is still to minimize the number of selected sets but with the additional constraints of:

$$\sum_{j=1}^m b_{ij} x_j \geq 2 \quad \text{for } i = 1 \dots n \quad (3)$$



Since all nodes in the primary set are also in the backup set centered at the same server,  $b_{ij} = 1$  if  $a_{ij} = 1$ ; but we can not have a primary server also service the same node as the backup server — the constraint in (3) ensures the selection of a different server as the backup.

#### 4.1 LP Relaxation-based Methods

The above formulation can be approximated by first solving the LP relaxation of the problem optimally and then rounding the fractional values to integers. The LP relaxation of the problem is to allow the selection variables  $x_j$  to take fractional values between  $[0, 1]$ . The LP relaxation can be solved in polynomial time and the rounding can be done in  $O(n)$ . Reference [10] introduced a rounding algorithm which is a  $p$ -approximation algorithm, where  $p = \max_i \{\sum_j a_{ij}\}$  is the maximum number of sets covering an element. Although this worst case result is not very promising, we are more interested in the average case performance. We refer to the rounding algorithm in [10] as the *fixed-rounding (FR)* algorithm:

- Step 1: solve the LP relaxation of the problem and let  $\{x_j^*\}$  be the optimal solution;
- Step 2: output sets  $\{S_j | x_j^* \geq \frac{1}{p}\}$ .

The intermediate solution for the LP relaxation naturally provides a lower bound  $= \sum_j x_j^*$  for the set cover problem, since the fractional solution is an optimal solution and the LP relaxation is a super set of the set cover problem. We will use this lower bound to compare the algorithm performance in our simulations.

We have also devised an *incremental-rounding (IR)* algorithm that imposes more restricted rules while selecting sets based on the value of  $x_j^*$ . Whenever we select a set, we remove all the elements that satisfy the covering constraint in (2) due to the newly selected set. Let  $M$  denote the union of all elements covered after each step. For the remaining uncovered elements in a set  $S_j$ , we compute  $p_j = \max_i \{\sum_j a_{ij}\}$  for  $i \in S_j \setminus M$ . We select a set if its selection variable is greater than the inverse of  $p_j$ ; to break ties, we select the set that has the largest number of remaining uncovered nodes.

- Step 1: solve the LP relaxation of the problem and let  $\{x_j^*\}$  be the optimal solution;
- Step 2: select set  $S_j$  such that :
  - 2(a)  $S_j$  has the largest number of uncovered elements;
  - 2(b)  $x_j^* \geq \frac{1}{p_j}$ ;
- Step 3: repeat step 2 until all elements are covered.

The correctness of the algorithm holds; since for each uncovered node, at least one set having  $x_j^* \geq \frac{1}{\sum_j a_{ij}}$  and  $p_j \geq \sum_j a_{ij}$ . By selecting all sets whose value satisfies 2(b), we guarantee to cover all the

nodes. Further more, since  $p_j$  is non-increasing in each repetition and  $p_j \leq p$ , the set selection criterion is more restrict than that in the FR algorithm, which in turn reduces the number of sets selected. Although the worst case bound is the same for both algorithms, we observe from our simulations that the IR algorithm typically performs much better than the FR algorithm.

An alternative to the tie-break rule in 2(a) is to select the set with the greatest  $x_j^*$  value, since the larger the value of the selection variable, the more “essential” the set may be. For example, if a node is covered by a single set, then the selection variable of this set must be 1 and the set must be selected. However, most of our simulations show that rule 2(a) generally performs better than this alternative rule. One plausible explanation is that rule 2(a) is more objective in attempting to include as many uncovered nodes as possible, while the alternative rule first selects those more “essential” sets, which may not contain many nodes.

It is easy to see that both of the algorithms can still have redundant sets in the final solution. To prune these extra sets, we use a simple pruning algorithm as the final step to complete the set selection:

- Step 1: sort all selected sets in increasing order of set size;
- Step 2: starting from the smallest set, check if it can be removed without leaving any of its nodes uncovered.
- Step 3: repeat Step 2 until all sets are checked.

## 4.2 Greedy Heuristics

A greedy algorithm is usually attractive due to its simplicity. In [15, 17], Johnson and Lovász introduced a greedy algorithm for the set cover problem with an  $O(\log n)$  approximation ratio. The basic greedy attribute of the algorithm is to select a set at every step that contains the maximum number of uncovered elements. For the backup problem variance, we extend on that model by treating any node that has not satisfied the constraints of (2) and (3) as equally uncovered. At each step, we select a set that has the largest remaining uncovered nodes and repeat till there are no more uncovered nodes.

## 4.3 Comparison of the FR, IR and the Greedy Algorithms

We first compare our *incremental rounding (IR)* algorithm with the *fixed rounding (FR)* algorithm proposed in [10] and with the greedy algorithm. The results are further compared with the lower bound obtained as the optimal solution from the LP methods. The LP solver we used, is called PCx [4] which is an interior-point based linear programming package.

We use a simple setup to investigate the relative performance of these algorithms. The underlying network graph is a single graph of randomly distributed nodes on a 100 by 100 unit length map. The service range of a server is 20 units. Ideally, if nodes are perfectly positioned, this will give a solution of  $\lceil \frac{100}{40} \rceil \times \lceil \frac{100}{40} \rceil = 9$  selected servers regardless of the node density. The lower bound we obtained is indeed not far from the ideal and stays constant with the increase of the node density as shown in Figure 1.

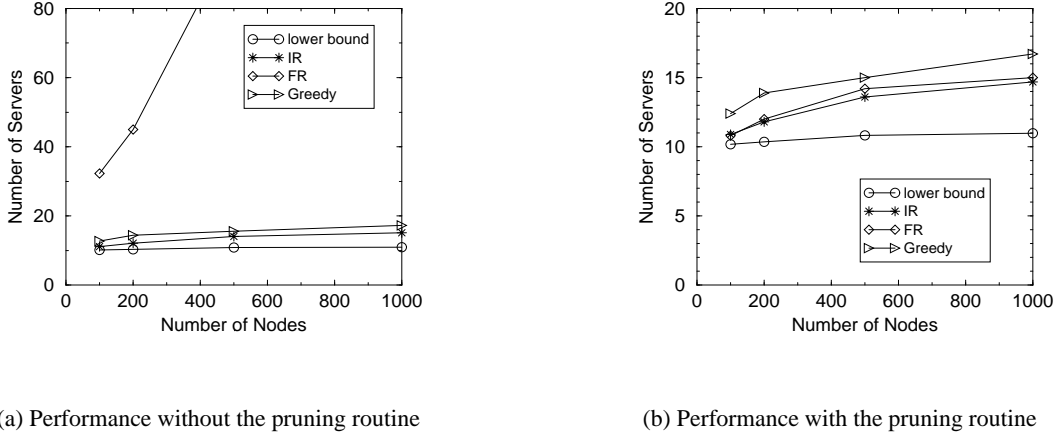


Figure 1: Comparison of the FR, IR and the Greedy Algorithms

We show the performance of the rounding algorithms with and without the pruning routine in Figure 1. As expected, the FR algorithm performs badly with the increase of node density, since the largest number of sets covering a node  $p$ , also increases with node density which makes the selection criterion less strict. On the other hand, the IR algorithm always is the closest to the lower bound. The FR algorithm does benefit greatly from the pruning routine, achieving performance closer to the lower bound, and is only slightly worse than the IR algorithm, but better than the greedy algorithm. This relative performance holds for other settings we have tried as well. In the rest of the paper, we will mainly focus on the IR algorithm to evaluate the placement methods in more complicated network configurations.

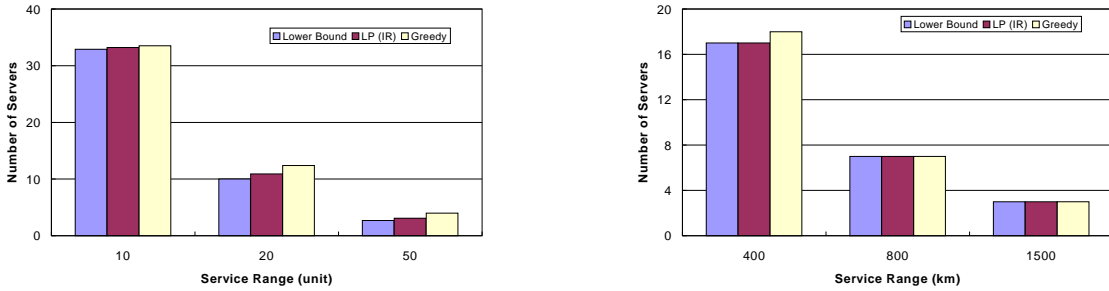
## 5 Simulation Results

It is most challenging to select a representative set of simulations that demonstrate the relations between the methodologies, the configurations and the results, given the vast number of parameters. In order to concentrate on a few aspects which we considered interesting, we have mostly used small and uniform

settings in the simulations presented in this section. We do not claim our network models capture all the fundamental characteristics of the Internet, but we hope the random networks and the geographic networks represent some degree of variances that allow us to examine the behavior of our methodology. Throughout the section, readers are referred to Table 1 for the interpretations of the parameters. Unless otherwise mentioned, we use the following default parameter values: the random graph scale is 100 by 100 units; the probability of network interconnection is 1.0 for both network configurations; the region size is 10 units and the co-location vicinity is two units in the random graph; the probability of including cities in the regional networks is 0.6 and 0.8 for national networks in the geographic networks.

### 5.1 Single Network

We first present results on a single network for both the random graph and the geographical graph. We perform simulation on the following three scenarios: (a)  $k = 1$ , when only one primary server is required to cover each node; (b)  $k = 1$  and with one backup server; (c)  $k = 1$  with relaxation on server to client distance. The last scenario is to allow remote client to connect to its nearest server, even the distance between them is over the threshold. This allows service providers to be more cost effective and not to install servers just for a few remotely located nodes. The relaxation is done by including every node in at least  $l$  server sets. That is, if a node does not have enough number of servers from the initial transformation due to its location, we include it in the next few nearest servers' sets till we reach  $l$  servers. The results for the random graph is the average over 10 runs, while the result for the geographic graph is from a single run, since the node locations are all fixed.

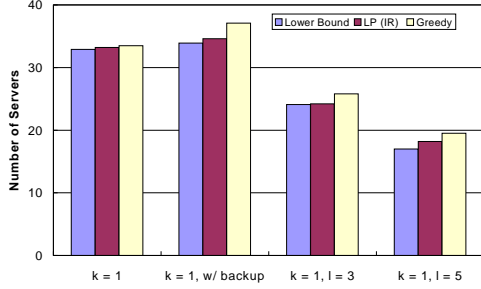


(a) Single Random Network: n = 100

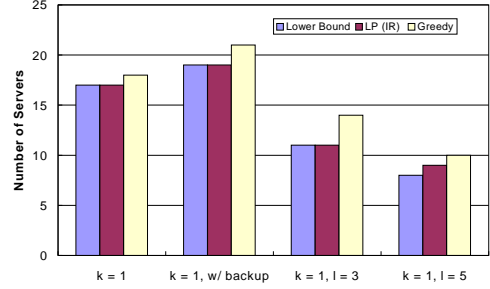
(b) Single Geographical Network: n = 50

Figure 2: Variation on Server Service Range

Figure 2 shows the number of required servers when varying service range. In general, both the IR and the greedy algorithm performs closely with the lower bound.



(a) Single Random Network:  $n = 100$ , scale = 100, range = 10



(b) Single Geographical Network:  $n = 50$ , range = 400 km

Figure 3: Variation on Different Service Requirement

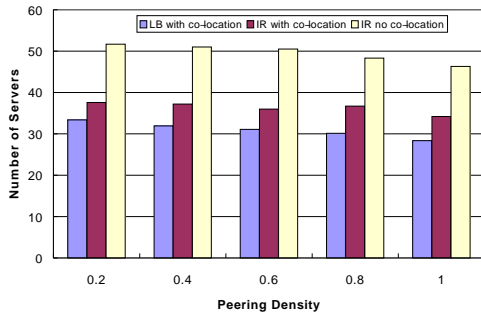
Figure 3 shows the performance against the different service requirements. The backup server range is twice that of the primary server for both networks. It shows that the addition of the backup servers only increases the number of total servers slightly. The service range relaxation is also effective in reducing number of servers to about 55% and 75% of the original number, with  $l = 3$  and  $l = 5$  respectively. However, the relaxation is useful only when the service range is small. In Figure 3, the service range is 10 units and 400 km in the two network configurations, which covers about 7% and 8% of the maximum distance in their respective networks. If we double the service range, we find that the relaxation becomes irrelevant since each node is likely included in multiple sets already. Table 2 shows the average node to server distance with and without the service range relaxation. Since there may be multiple servers covering a node, we select the closest server when computing the distance. The results for the random graph is the worst case among 10 runs.

	Random Graph (unit) range = 10			Geographic Graph (km) range = 400 km		
	mean	std.	max	mean	std.	max
$l = 0$	4.94	3.74	9.83	167.49	140.11	398.79
$l = 3$	6.30	4.47	14.82	259.78	222.65	1013.42
$l = 5$	8.45	5.56	25.36	304.69	238.59	1114.78

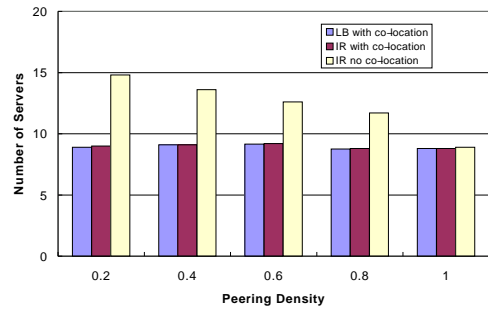
Table 2: Average Client to Server distance

## 5.2 Multiple Networks

In this section, we study the relations between server placement and the density of network peering links. We refer to “peering links” as both the peering and transit relationship between two ISPs. As these links aggregate and transport traffic from one domain to another, their limited capacities contribute significantly to the user experienced network congestion. Additionally, these network exchange points may locate off the optimal path, resulting longer and more circuitous routes. One way to circumvent these congestion points is to use co-location services, where servers can access multiple networks and can route traffic directly to these networks without going through the exchange points. We demonstrate the relative performance with and without server co-locations in Figure 4.



(a) Random Network: 5 networks, 100 nodes per network, range = 20 units



(b) Geographic Networks: 5 regional networks, 1 national networks, total nodes = 96, range = 800 km

Figure 4: Variation on Network Peering Density

Peering Density	Random Network			Geographic Network		
	5 networks, 100 nodes per network			5 regional, 1 national network, total 96 nodes		
	total links	co-location	no co-location	total links	co-location	no co-location
0.2	83.05	22.16%	38.77%	11.6	17.24%	80.17%
0.4	158.05	23.28%	37.52%	18.9	10.05%	82.54%
0.6	238.60	21.42%	38.98%	27.4	6.20%	82.48%
0.8	317.75	22.19%	35.22%	36.3	8.82%	90.36%
1.0	410.1	21.24%	35.94%	45.2	7.30%	96.90%

Table 3: Number of Peering Links In Use

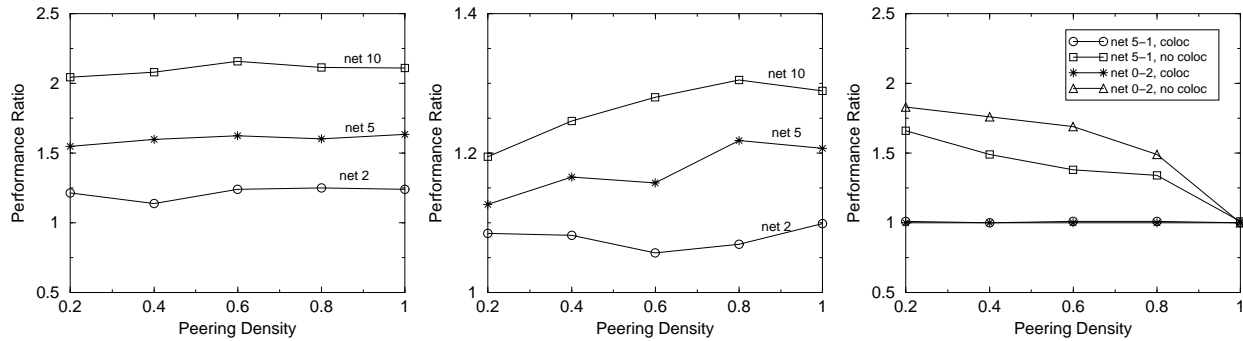
For this simulation, we use two network configurations: one is 5 random graphs, the other is the geographic networks consisting of 5 regional networks and 1 national network. Hereafter, we will use the term  $m$ - $n$  to denote the geographic networks consisting of  $m$  regional networks and  $n$  national networks. We use  $TX_p = 1$ , so every pair of networks are always interconnected, unless they do not have any common presences in any of the peering regions. The x-axis in Figure 4 decides the number of peering regions of two networks. For random graph, a region is a fixed size grid dividing the total graph scale; from a peering region, we select a closest pair of nodes to interconnect. For geographic graph, a region is a metropolitan area.

Figure 4 shows the number of required servers for the lower bound with co-location and the IR algorithm with and without co-location. The co-location service reduces the number of required servers by as much as 50% when peering is sparse. The geographic graph appears to be more sensitive to the peering density, as the performance of IR no co-location approaches the lower bound when peering density approaches 1. This is due to that the peering link is “cheaper” in a geographic network than in a random network. In the geographic network, two networks peer only if they both have presences in the same metropolitan area, which results the delay on the peering link to be 0. Contrarily, the peering link has a positive delay in the random graphs which adds to the server to client delay. Additionally, the “hot-potato” routing policy always selects the closest peering link rather than the one with the lowest delay. These combined effects shows that unless peering can guarantee a high level of quality, merely increase the peering density does not help reducing the client access delay. Table 3 summarizes the number of links used in the two scenarios.

Figure 5 shows the relative performance ratio of the IR algorithm, with and without co-location, against the lower bound. We varied the number of random networks as 2, 5 and 10 and used two configurations for the geographic networks: 5-1 and 0-2. The results are mostly consistent with that in Figure 4. Additionally, it suggests that on the random networks, the performance of non co-located servers worsens much more with the increase of the number of networks, as compared to the performance of co-located servers.

### 5.3 Server Load

Throughout this paper, we assumed that the cost of installing and operating a separate server far out weights the cost of buying more bandwidth at a location. In fact, in order to be more cost effective, we are more interested in how under utilized a server can be, that is what is the lowest fraction of clients served by a single server.



(a) Random Network without co-location: range = 20, 100 nodes per network.

(b) Random Network with co-location: range = 20, 100 nodes per network.

(c) Geographic Networks: range = 800 km.

Figure 5: Relative Performance Ratio Against Lower Bound

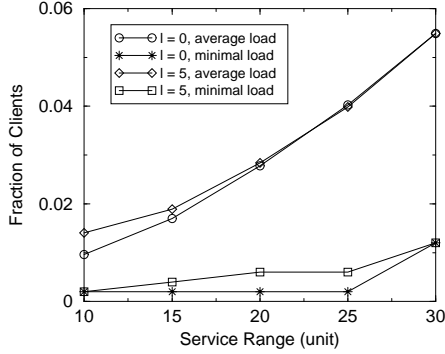
Figure 6 shows the average and minimal server load distribution under the IR algorithm with co-location. As expected, the average server load increases with the increase of service range. The load distribution is more even on the random networks than on the geographic networks due to the different node distribution: the geographic networks have significantly higher node density on the east side than on the west side.

However, the minimal load does not lift as much for both networks. It is easier to understand this effect in the geographic networks, since a few metropolitan areas, such as Seattle and Portland, are more segregated from the rest of the areas. Consequently, it requires at least one server to cover and only cover these two areas. Although it is less obviously to be so in the random networks, it seems there are always a small number of nodes that are particularly further away from the rest of the group. The curves labeled  $l = 5$  indicates the average and minimal fraction of clients served by a single server when we enforce each node to be included in at least 5 server sets. The increase of the minimal server load from the relaxation is more visible in the geographic networks than in the random networks.

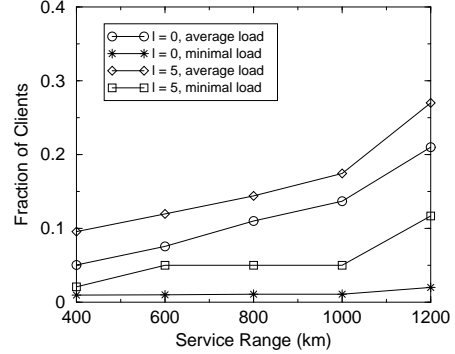
## 5.4 Computation Complexity

Although linear programming methods are widely practiced in areas such as operational research and management, its application in network design is less prevalent. This often attributes to its complexity and its lack of scalability to solve large problem instances. The server placement problem in overlay networks, on the other hand, generally has instances of smaller sizes, roughly on the order of hundreds, due to the heavy





(a) Random Network, 5 nets, 100 nodes per network, peering density = 0.4.



(b) Geographic Networks, 5-1 nets, total 96 nodes, peering density = 0.4.

Figure 6: Characteristics of Server Load

geographical aggregation of client representations. In this section, we quantify the computation time for the IR algorithm and compare it with the greedy algorithm. The implementation of the greedy algorithm is not optimized but it provides us a basic idea of the computation intensity with the variance on instance sizes.

We ran the simulation over three network configurations for each type of graphs. The network configurations are chosen to be of small, medium and large instance sizes, in terms of number of network nodes. The largest instance size is beyond the range of what we considered as potential server locations for overlay networks, nevertheless, we present it to characterize the algorithm complexity.

Table 4 summarizes the running time of the algorithms, which includes the solving time of the IR algorithm or the greedy algorithm and the time for the pruning routine. In general, the IR algorithm is very time consuming especially for large instance sizes. This is particularly true for the geographic networks, as the time of the greedy algorithm increases only slightly from net 25-5 to net 250-10, while the time of the IR algorithm grows much faster. One explanation is that, when there is co-location, the number of sets is fixed at 50, one for each metro area, but the set size changes with the number of network nodes. In this case, the greedy algorithm is able to eliminate a large number of nodes for each selected sets, while for the LP methods, it does not take such progressive approach, resulting in a tremendous amount of computation time.

Throughout our simulations, the greedy algorithm always requires about 5% to 15% more servers than that of the IR algorithm. Though this maybe tolerable in some cases, it could represent a large sum of additional server cost. On the other hand, the IR algorithm, although not as simple as the greedy algorithm,

	Random Graph			Geographic Graph		
	net 1	net 10	net 50	net 5-1	net 25-5	net 250-10
Avg. nodes	100	567	2978	87	430	2652
IR	0.08	1.85	468.75	0.06	1.00	428.14
Greedy	0.01	0.83	18.39	0.01	0.02	0.10

Table 4: Computation Time of the IR and Greedy Algorithms (secs)

can solve up to a reasonable problem size without being overwhelmingly time consuming. Therefore, when conducting infrequent network design processes, the IR algorithm has the ultimate advantage of cost savings.

## 6 Conclusions

We have presented a server placement method in overlay networks as an application of the set cover problem. The placement satisfies constraints on the server to client paths, which indicate the achievable service qualities along the path. We expect that network provisioning for quality of service becomes more common as the Internet continues to grow; and such an automated methodology is useful for service providers to analyze the potential cost of network provisioning.

We solved the set cover problem using methods based on linear programming relaxation as well as greedy heuristics. We also presented an incremental integer rounding algorithm for the LP-relaxation based method. Our network settings model explicitly the presence of co-location services, which have become increasingly popular for business corporations to out source their data servers. Our results indicate co-location can save up to 50% of the server installation cost. We also presented variance of the simple set cover problem to allow backup servers and to allow distance relaxation. These variances brings opportunities to provide more cost effective services. Through simulation, we studied the behavior of the algorithms under various network settings and observed the implication of network peering density and the characteristics of server load distributions. Although, LP-relaxation based methods are traditionally considered as too expensive and complex to solve any practical problems, we find that it is suitable and effective for our overlay network models and results in better performance than that of the greedy algorithm.

## A Geographic Categorization of Metropolitan Areas

**Region north\_central[17]** = "Chicago, IL", "Detroit, MI", "Cleveland, OH",  
"Minneapolis, MN", "St. Louis, MO", "Denver, CO",  
"Cincinnati, OH", "Kansas City, MO", "Milwaukee, WI",  
"Indianapolis, IN", "Columbus, OH", "Salt Lake City, UT",  
"Nashville, TN", "Memphis, TN", "Oklahoma City, OK",  
"Grand Rapids, MI", "Louisville, KY";

**Region north\_east[21]** = "New York, NY", "Chicago, IL", "Washington, DC",  
"Philadelphia, PA", "Boston, MA", "Detroit, MI",  
"Cleveland, OH", "Pittsburgh, PA", "Cincinnati, OH",  
"Milwaukee, WI", "Virginia Beach, VA", "Indianapolis, IN",  
"Columbus, OH", "Charlotte, NC", "Greensboro, NC",  
"Buffalo, NY", "Hartford, CT", "Providence, RI",  
"Rochester, NY", "Raleigh, NC", "Richmond, VA";

**Region west[10]** = "Los Angeles, CA", "San Francisco, CA", "Seattle, WA",  
"Phoenix, AZ", "San Diego, CA", "Denver, CO",  
"Portland, OR", "Sacramento, CA", "Las Vegas, NV",  
"Salt Lake City, UT";

**Region south\_central[12]** = "Dallas, TX", "Houston, TX", "Atlanta, GA",  
"Phoenix, AZ", "St. Louis, MO", "Kansas City, MO",  
"San Antonio, TX", "New Orleans, LA", "Nashville, TN",  
"Austin, TX", "Memphis, TN", "Oklahoma City, OK";

**Region south\_east[15]** = "Atlanta, GA", "Miami, FL", "St. Petersburg, FL",  
"Virginia Beach, VA", "Orlando, FL", "Charlotte, NC",  
"New Orleans, LA", "Greensboro, NC", "Nashville, TN",  
"Memphis, TN", "Raleigh, NC", "Jacksonville, FL",  
"West Palm Beach, FL", "Louisville, KY", "Richmond, VA";

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